

OPG'S

Practice Problem Series

Based on Coordinate Geometry

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- Q01.** What does the equation $x^2 + y^2 - 6x + 8y + 25 = 0$ represent? Explain.
- Q02.** Find radius of a circle which passes through $(6, 2)$, and two of whose diameters are lying on the lines $x + y = 6$ and $x + 2y = 4$.
- Q03.** Write radius of circle $4x^2 + 4y^2 - 10x + 5y + 5 = 0$.
- Q04.** The line $x + 3y = 0$ is a diameter of the circle $x^2 + y^2 - 6x + 2y = 0$. True or False?
- Q05.** The circle $x^2 + y^2 - 6x + 2y = 0$ passes through the origin. Give the equation of one of its diameter.
- Q06.** What is the area of the circle which is centred at $(1, 2)$ and is passing through $(4, 6)$?
- Q07.** Locate the centre of $(x - a)(x - c) + (y - b)(y - d) = 0$.
- Q08.** Write the centre of a circle passing through the points $(0, 0)$, $(a, 0)$ and $(0, b)$.
- Q09.** If the equation $ax^2 + by^2 + 2hxy + 2gx + 2fy + c = 0$ represents circle, write the condition(s) on a, b, c, f, g and h .
- Q10.** The lines $2x - 3y = 5$ and $3x - 4y = 7$ are diameters of a circle of area 154sq. units . Write the equation of this circle.
- Q11.** The point $(1, 2)$ lies inside the circle given as $x^2 + y^2 - 2x + 6y + 1 = 0$. True/ false?
- Q12.** What is the length of a chord lying along the line $3x + 4y = 15$ for the circle $x^2 + y^2 = 36$?
- Q13.** Write the equation of a line passing through $(1, -2)$ and which cuts off equal intercepts from the axes.
- Q14.** Determine the angle between lines $2x + 3 = 0$ & $3y - 5 = 0$.
- Q15.** For what value of a the lines $3x - 4y + 7 = 0$ and $ax + 6y + 1 = 0$ are perpendicular?
- Q16.** Locate the image of $(-1, 3)$ on the line $x = y$.
- Q17.** Image of $(4, -6)$ by a line mirror is $(2, 1)$ then, find the equation of this line mirror.
- Q18.** Write the equation of a straight line which is passing through the intersection of $3y = x + 1$ and $2x + 5y = 9$ and having infinite slope.
- Q19.** The straight line $5x + 4y = 0$ passes through the point of intersection of the straight lines given by $2x + y + 5 = 0$ and $x + 2y = 10$. True/ False?
- Q20.** Name the type of triangle formed by lines $y + x = 0$, $3x + y = 4$ and $x + 3y = 4$.
- Q21.** If the lines $3y + 4x = 1$, $y = x + 5$ and $5y + bx = 3$ are concurrent, then find the value of b .
- Q22.** Write the area enclosed by $|x| + |y| = 1$.
- Q23.** What is the length of \perp^{er} drawn from $(1, 2)$ upon the straight line $3x - 4y + 15 = 0$?
- Q24.** What will be the distance between the two lines $3x + 4y = 6$ and $6x + 8y = 15$?
- Q25.** Write the locus of the mid-point of the portion which is intercepted between the axes by $x \cos \alpha + y \sin \alpha = p$, where p is a constant.
- Q26.** If the straight line $6x - y + 2 + k(2x + 3y + 13) = 0$ is parallel to x -axis, find the value of k .
- Q27.** Write all the points on the line $2x + 5y + 4 = 0$ that lie at unit distance from the straight line $12x + 5y = 13$.
- Q28.** Write the coordinates of foot of \perp^{er} from the point $(2, 4)$ on the straight line $x + y = 1$.

- Q29. The distance between the foci of an ellipse is known to be 10units and its latus-rectum is 15. Find equation of such an ellipse.
- Q30. Find the equation of an ellipse in the standard form whose minor axis is equal to the distance between the foci and whose latus-rectum is 10.
- Q31. The value of e for an ellipse is $\frac{1}{2}$ and the distance between its foci is 4units. Find its equation.
- Q32. Find the equation to the ellipse whose foci are $(4,0)$ and $(-4,0)$ having eccentricity as $\frac{1}{3}$.
- Q33. Write the equation of an ellipse, referred to its axes as x, y axes respectively, which passes through the point $(-3,1)$ and has the eccentricity $\sqrt{\frac{2}{3}}$.
- Q34. Find the eccentricity of an ellipse if its latus-rectum is half of its major axis.
- Q35. Find the eccentricity of an ellipse if its latus-rectum is one-third of its major axis.
- Q36. Determine the equation of a hyperbola whose conjugate axis is 5 and the distance between the foci is 13 units.
- Q37. Determine the equation of the hyperbola if the distance between the foci is 9 units and eccentricity is $\sqrt{3}$.
- Q38. The coordinates of the foci of a hyperbola are given as $(\pm 6,0)$ and it is also provided that the latus-rectum is of length 10units. Find its equation.
- Q39. Find the equation to the hyperbola referred to its axes as co-ordinate axes whose conjugate axis is 7 and passes through the point $(3,-2)$.
- Q40. Find the locus of a point which moves in such a way that the difference of its distances from the points $(-5,0)$ and $(5,0)$ is equal to 8.
- Q41. Find the equation of a hyperbola whose foci are at $(0, \pm \sqrt{10})$ and which passes through $(2,3)$.
- Q42. Write the equation of a hyperbola, the length of whose latus-rectum is found to be 8units and eccentricity is $\frac{3}{\sqrt{5}}$.
- Q43. If the parabola $y^2 = 4ax$ passes through $(3, 2)$ then, write its length of latus-rectum.
- Q44. The end points of the latus-rectum of a parabola are $(7, \pm 5)$. Write its equation.
- Q45. Check if the point whose coordinates are given by $(b \cos \alpha, a \sin \alpha)$ lie on $\frac{x^2}{b^2} + \frac{y^2}{a^2} = 1$?

❖ ANSWERS ❖

- Q01. A point circle centered at $(3, -4)$ Q02. $2\sqrt{5}$ units Q03. $\frac{3\sqrt{5}}{8}$ units
- Q04. True Q05. $x + 3y = 0$ Q06. 25π Sq.units Q07. $\left(\frac{a+c}{2}, \frac{b+d}{2}\right)$
- Q08. $\left(\frac{a}{2}, \frac{b}{2}\right)$ Q09. $a = b; h = 0; a, b, g, f, c \in \mathbb{R}$ Q10. $x^2 + y^2 - 2x + 2y - 47 = 0$
- Q11. False Q12. $6\sqrt{3}$ units Q13. $x - y - 3 = 0, x + y + 1 = 0$
- Q14. $\frac{\pi}{2}$ Q15. 8 Q16. $(3, -1)$ Q17. $4x - 14y = 47$
- Q18. $x = 2$ Q19. True Q20. Isosceles triangle Q21. 6
- Q22. 2 Sq.units Q23. 2 units Q24. $\frac{3}{10}$ units
- Q25. $x^2 + y^2 = p^2 \operatorname{cosec}^2 \alpha$, A circle of radius $p \operatorname{cosec} \alpha$ and centered at $(0, 0)$
- Q26. -3 Q27. $(3, -2), \left(\frac{2}{5}, -\frac{24}{25}\right)$ Q28. $\left(-\frac{1}{2}, \frac{3}{2}\right)$
- Q29. $\frac{x^2}{100} + \frac{y^2}{75} = 1$ Q30. $x^2 + 2y^2 = 100$ Q31. $\frac{x^2}{16} + \frac{y^2}{12} = 1$ Q32. $\frac{x^2}{144} + \frac{y^2}{128} = 1$
- Q33. $x^2 + 3y^2 = 12$ Q34. $\frac{1}{\sqrt{2}}$ Q35. $\sqrt{\frac{2}{3}}$ Q36. $\frac{x^2}{144} - \frac{y^2}{25} = \frac{1}{4}$
- Q37. $4x^2 - 2y^2 = 27$ Q38. $\frac{x^2}{16} - \frac{y^2}{20} = 1$ Q39. $65x^2 - 36y^2 = 441$ Q40. $\frac{x^2}{16} - \frac{y^2}{9} = 1$
- Q41. $y^2 - x^2 = 5$ Q42. $4x^2 - 5y^2 = 100$ Q43. $\frac{4}{3}$ units Q44. Self
- Q45. Yes the point lies on the given curve.

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☞ For any clarification(s), please contact on any of the followings :

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